



Coimisiún na Scrúduithe Stáit
State Examinations Commission

Leaving Certificate Examination, 2012
Sample Paper

Mathematics

(Project Maths – Phase 3)

Paper 1

Ordinary Level

Time: 2 hours, 30 minutes

300 marks

Examination number

Centre stamp

Running total	
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For examiner	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
Total	

Grade

Instructions

There are **two** sections in this examination paper:

Section A	Concepts and Skills	150 marks	6 questions
Section B	Contexts and Applications	150 marks	3 questions

Answer all nine questions.

Write your answers in the spaces provided in this booklet. There is space for extra work at the back of the booklet. You may also ask the superintendent for more paper. Label any extra work clearly with the question number and part.

The superintendent will give you a copy of the booklet of *Formulae and Tables*. You must return it at the end of the examination. You are not allowed to bring your own copy into the examination.

Marks will be lost if all necessary work is not clearly shown.

Answers should include the appropriate units of measurement, where relevant.

Answers should be given in simplest form, where relevant.

Write the make and model of your calculator(s) here:

Question 4

(25 marks)

- (a) Solve the equation $x^2 - 6x - 23 = 0$, giving your answer in the form $a \pm b\sqrt{2}$, where $a, b \in \mathbb{Z}$.

- (b) Solve the simultaneous equations

$$2r - s = 10$$

$$rs - s^2 = 12$$

Question 5

(25 marks)

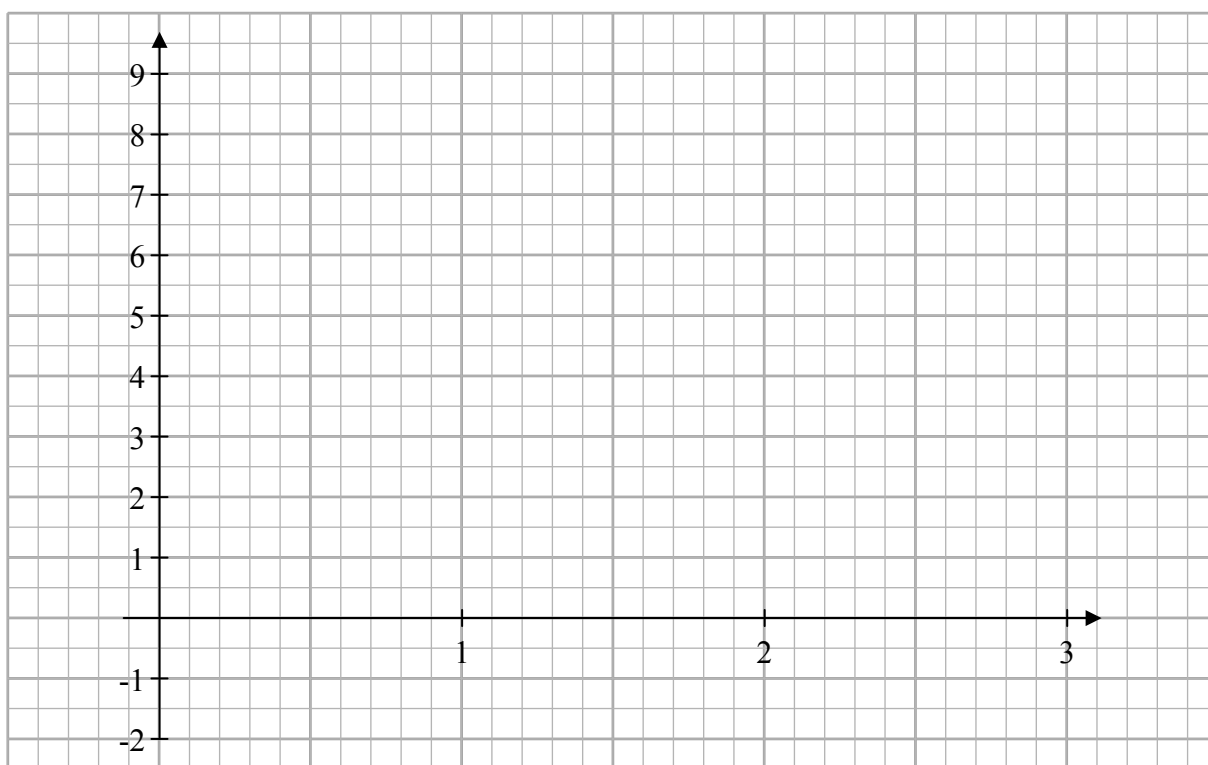
Two functions f and g are defined for $x \in \mathbb{R}$ as follows:

$$f : x \mapsto 2^x$$

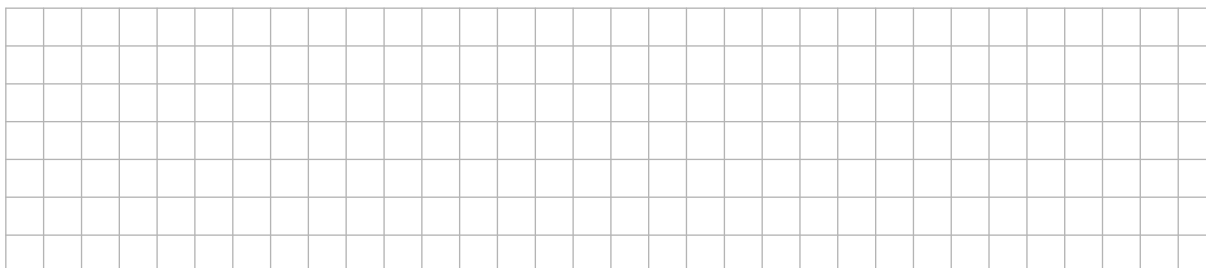
$$g : x \mapsto 9x - 3x^2 - 1$$

(a) Complete the table below, and use it to draw the graphs of f and g for $0 \leq x \leq 3$.

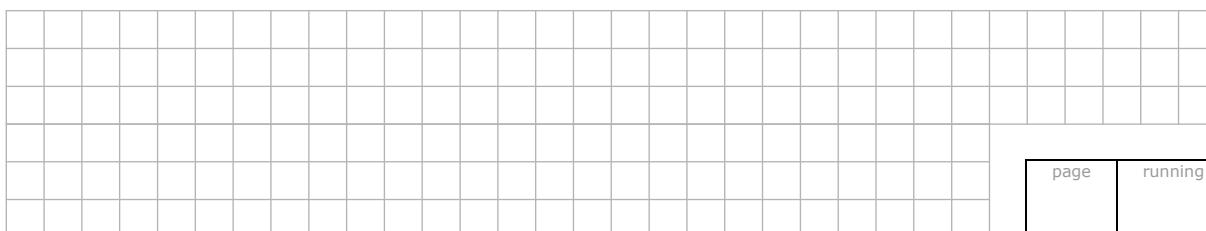
x	0	0.5	1	1.5	2	2.5	3
$f(x)$							
$g(x)$							



(b) Use your graphs to estimate the value(s) of x for which $2^x + 3x^2 - 9x + 1 = 0$.



(c) Let k be the number such that $2^k = 6$. Using your graph(s), or otherwise, estimate $g(k)$.



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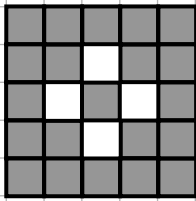
Answer **all three** questions from this section.

Question 7

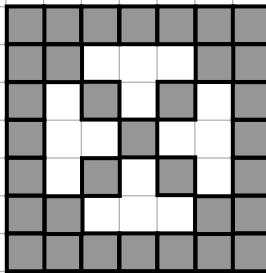
(50 marks)

Sile is investigating the number of square grey tiles needed to make patterns in a sequence. The first three patterns are shown below, and the sequence continues in the same way. In each pattern, the tiles form a square and its two diagonals. There are no tiles in the white areas in the patterns – there are only the grey tiles.

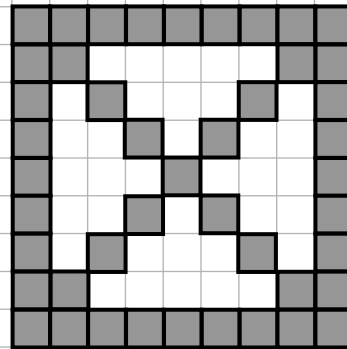
(Questions start overleaf.)



1st pattern



2nd pattern



3rd pattern

- (a) In the table below, write the number of tiles needed for each of the first five patterns.

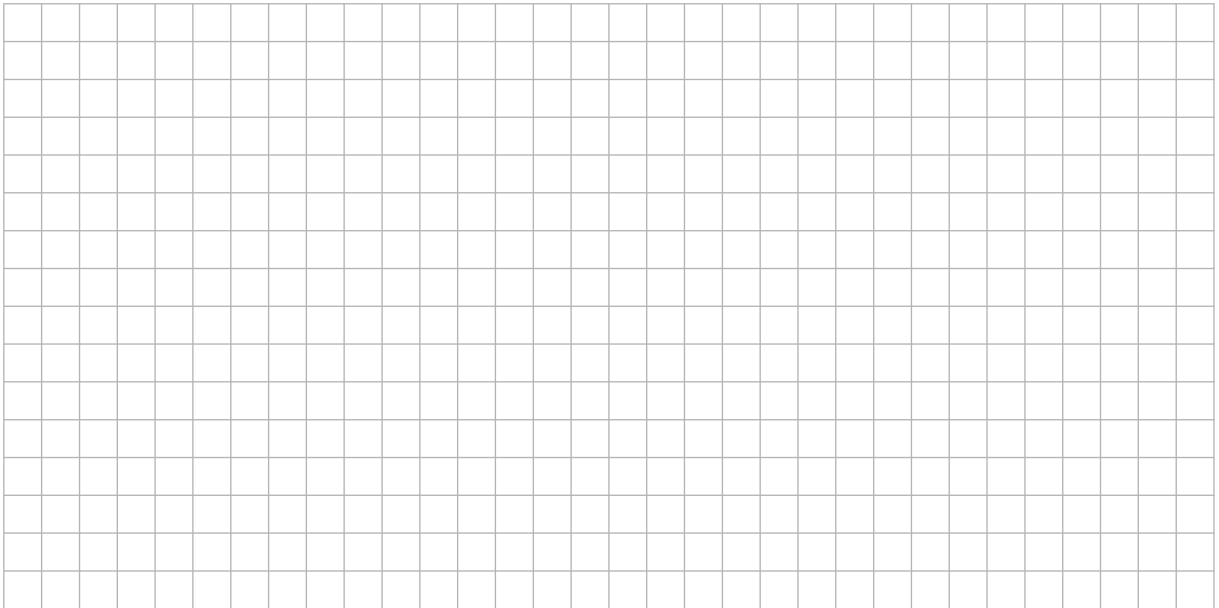
Pattern	1	2	3	4	5
No. of tiles	21	33			

- (b) Find, in terms of n , a formula that gives the number of tiles needed to make the n th pattern.

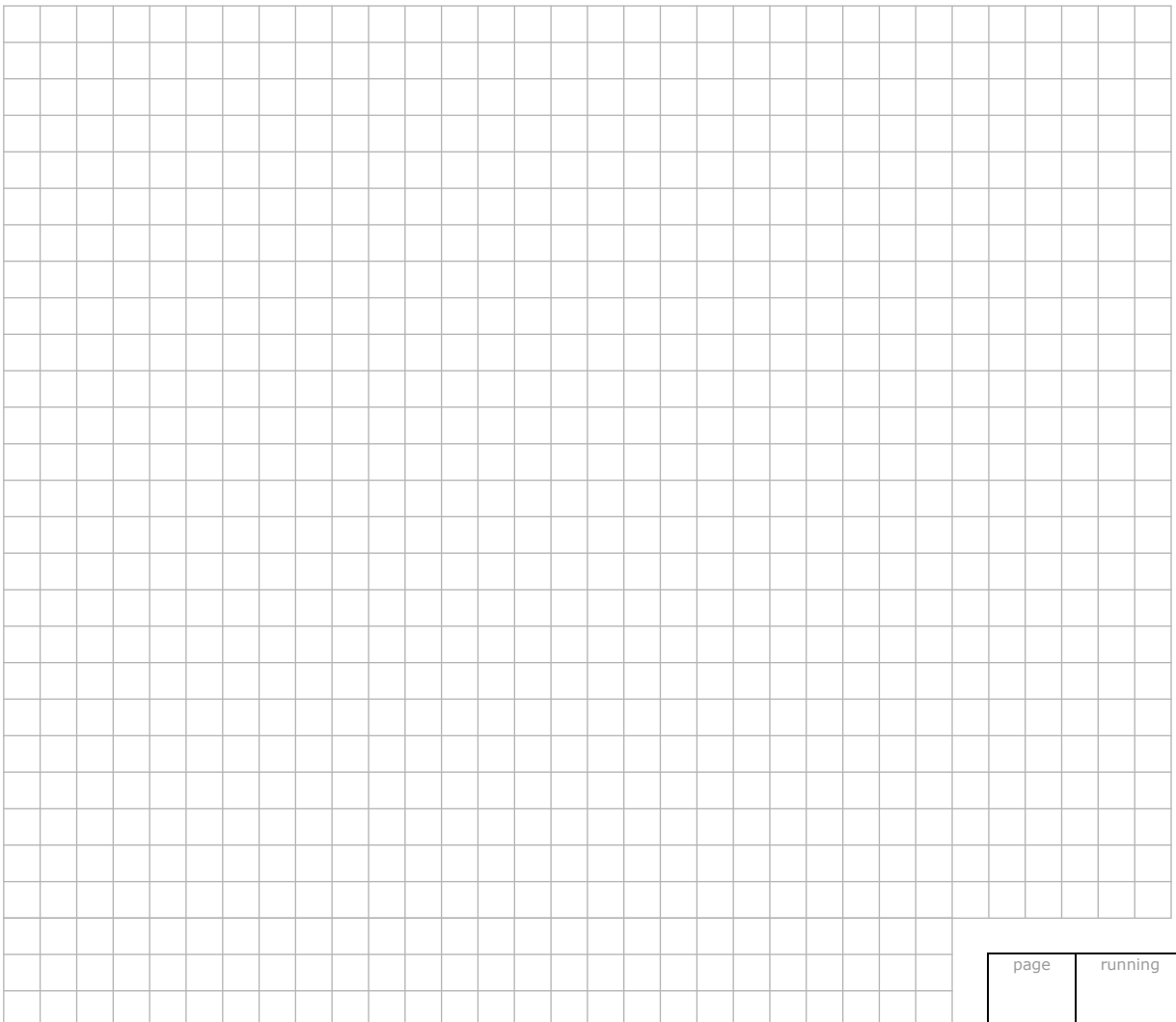
- (c) Using your formula, or otherwise, find the number of tiles in the tenth pattern.

- (d) Síle has 399 tiles. What is the biggest pattern in the sequence that she can make?

- (e) Find, in terms of n , a formula for the total number of tiles in the first n patterns.



- (f) Sile starts at the beginning of the sequence and makes as many of the patterns as she can. She does not break up the earlier patterns to make the new ones. For example, after making the first two patterns, she has used up 54 tiles, $(21 + 33)$. How many patterns can she make in total with her 399 tiles?



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- (c) John assumes that the plants will continue to grow at the same rates. Draw graphs to represent the heights of the two plants over the first *four weeks*.

(Questions continue overleaf.)



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- (b) A marble is dropped from the top of a fifteen-story building. The height of the marble above the ground, in metres, after t seconds is given by the formula:

$$h(t) = 44.1 - 4.9t^2.$$

Find the speed at which the marble hits the ground.

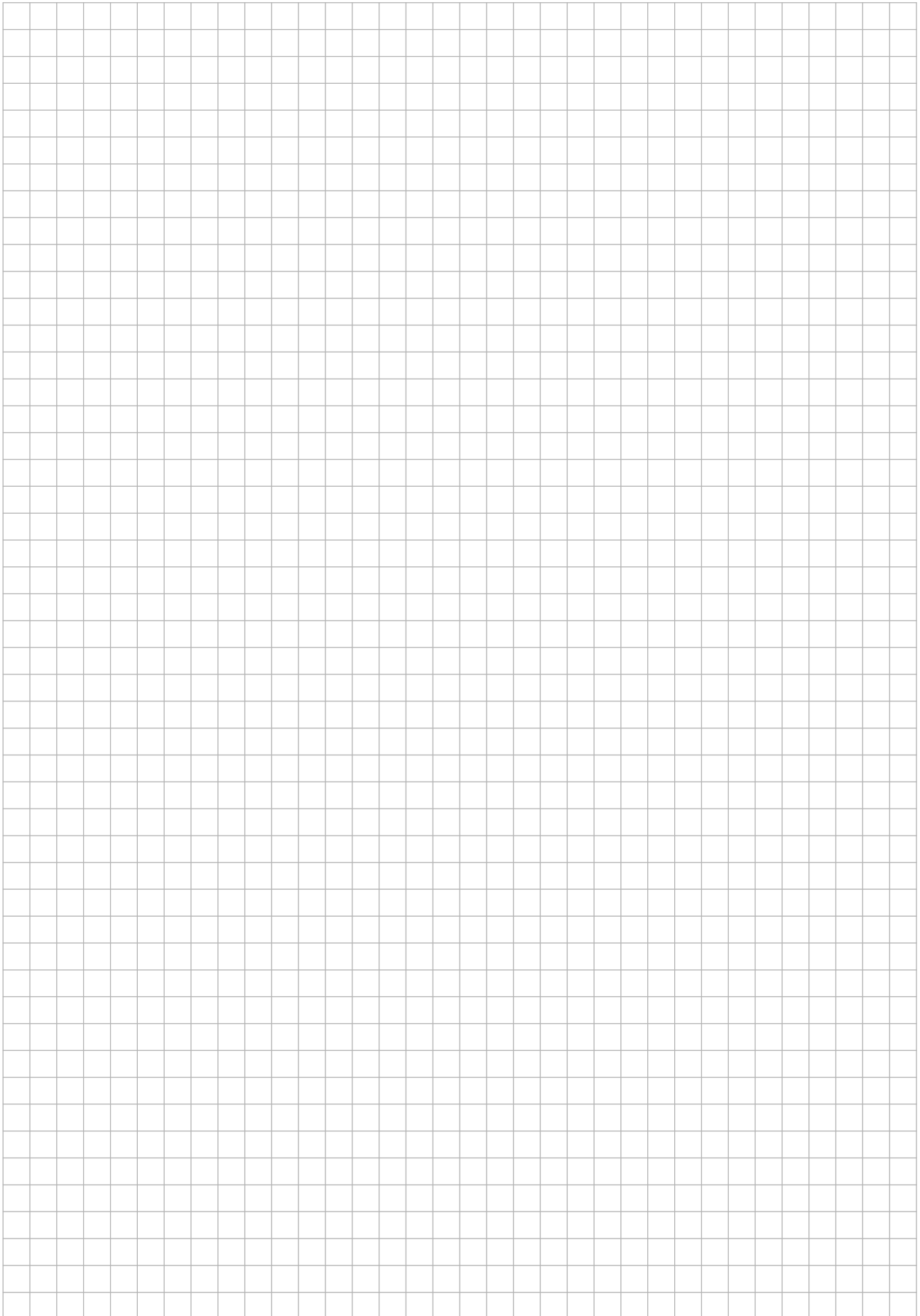
Give your answer (i) in metres per second, and

(ii) in kilometres per hour.

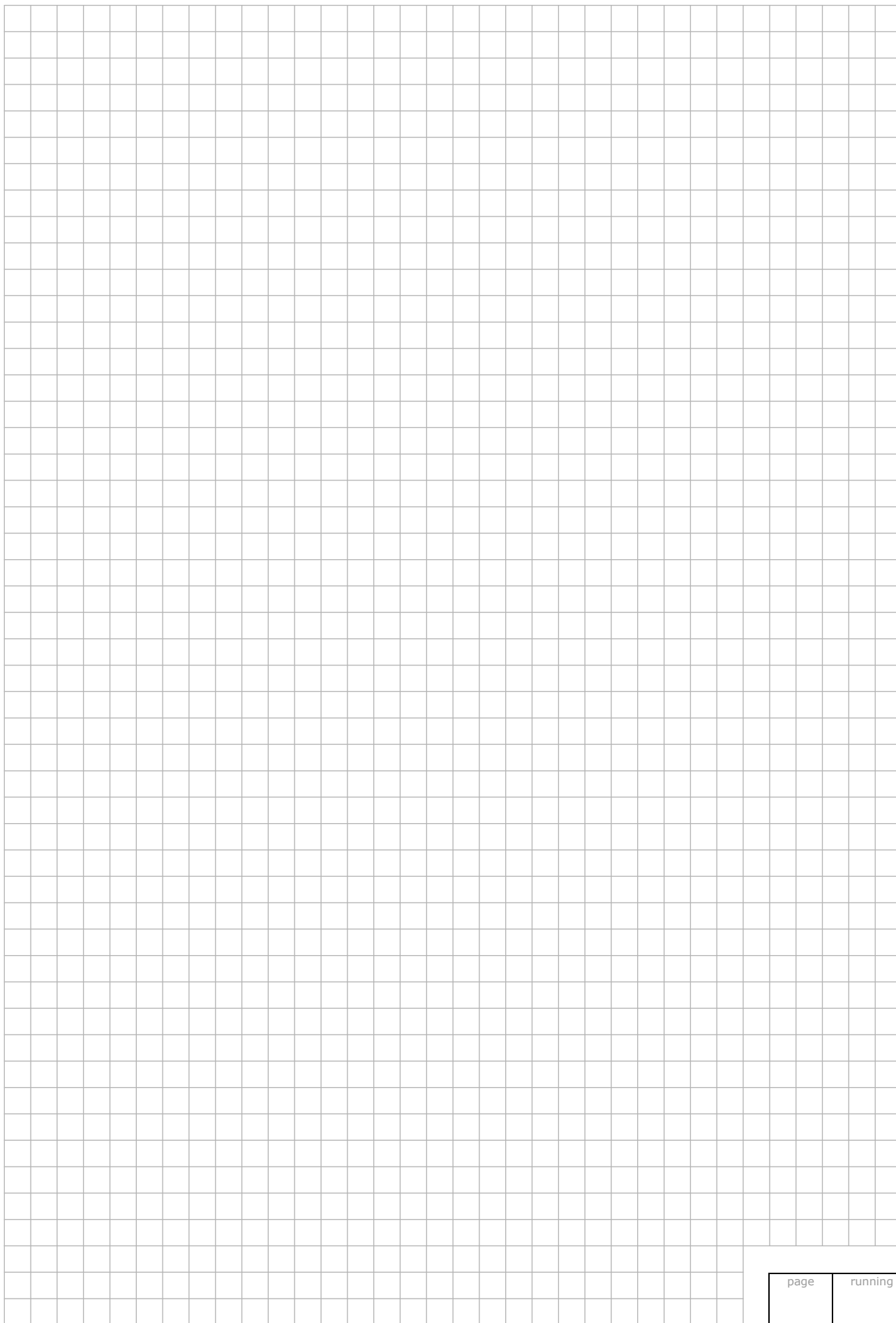


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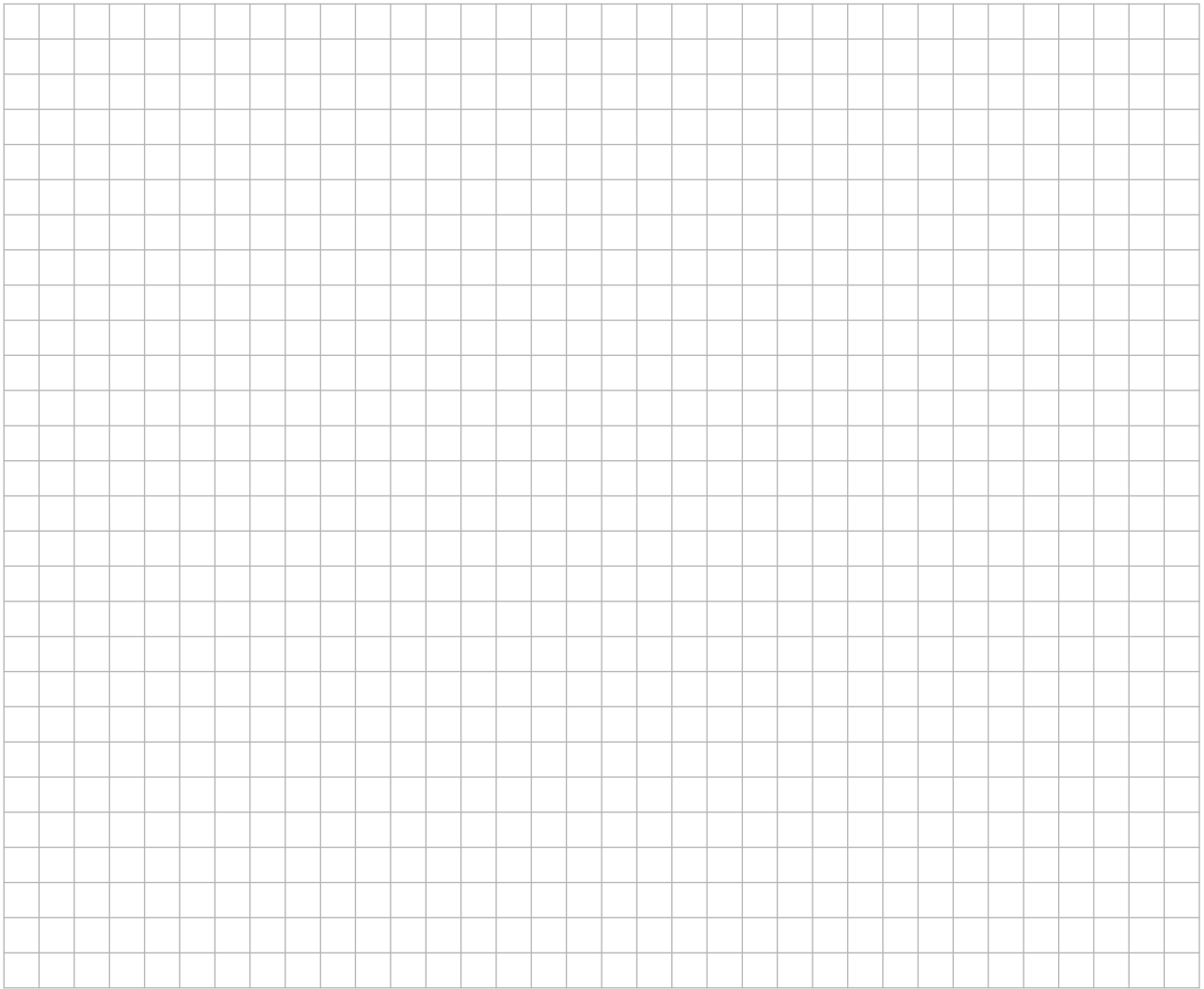
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Note to readers of this document:

This sample paper is intended to help teachers and candidates prepare for the June 2012 examination in the *Project Maths* initial schools. The content and structure do not necessarily reflect the 2013 or subsequent examinations in the initial schools or in all other schools.

Leaving Certificate 2012 – Ordinary Level

Mathematics (Project Maths – Phase 3) – Paper 1

Sample Paper

Time: 2 hours 30 minutes